MATHEMATICS



DPP No. 23

Total Marks: 31

Max. Time: 35 min.

Topics: Continuity & Derivability, Function, Limits, Quadratic Equation, Trigonometric Ratio

Type of Questions		M.M.	., Min.
Single choice Objective (no negative marking) Q.1,2	(3 marks, 3 min.)	[6,	6]

Multiple choice objective (no negative marking) Q.3 Subjective Questions (no negative marking) Q.4,5,6,7,8

(5 marks, 4 min.) 4] (4 marks, 5 min.) Ī20. 251

If $f(x) = \frac{a\cos x - \cos bx}{x^2}$, $x \ne 0$ and f(0) = 4 is continuous at x = 0, then the ordered pair (a, b) is 1. $(A) (\pm 1, 3)$ (C)(-1, -3)(D) (-1, 3) $(B)(1, \pm 3)$

2. Let A = $\{9, 10, 11, 12, 13\}$ and f: A \rightarrow N be a function defined as f(x) = Highest prime factor of x. Then number of elements in the range of f(x) is :-

(A)5

(B) 4

(C) 3

(D) None of these

Which of the statements(s) is/are INCORRECT? 3.

(A) If f + g is continuous at x = a, then f and g are continuous at x = a.

(B) If $\lim_{x\to a}$ (f g) exists, then $\lim_{x\to a}$ f and $\lim_{x\to a}$ g both exists.

(C) Discontinuity at x = a

non existences of limit

(D) All functions defined on a closed interval attain maximum or a minimum value in its interval.

4. Evaluate 6

(i) $\lim_{x\to 0} \frac{\cos(xe^x)-\cos(xe^{-x})}{y^3}$ (ii) $\lim_{x\to 0} (\cos ax)^{\cos ec^2bx}$

5. Evaluate:

(i)
$$\lim_{x\to 2a^+} \frac{\sqrt{x-2a} + \sqrt{x} - \sqrt{2a}}{\sqrt{x^2 - 4a^2}}$$

(i)
$$\lim_{x \to 2a^+} \frac{\sqrt{x - 2a} + \sqrt{x} - \sqrt{2a}}{\sqrt{x^2 - 4a^2}}$$
 (ii) $\lim_{x \to 0^+} \left(\frac{e^{x \ln(2^x - 1)} - (2^x - 1)^x \sin x}{e^{x \ln x}} \right)^{1/x}$

Find the sum of an infinite geometric progression whose first term is the limiting value of the function 6.

 $f(x) = \frac{\sin\left(x - \frac{\pi}{6}\right)}{\sqrt{3} \cos x}$ at $x = \frac{\pi}{6}$ and whose common ratio is the limiting value of the function

$$g(x) = \frac{\sin(x)^{1/3} \ln (1+3x)}{(\arctan \sqrt{x})^2 \left(e^{5 \cdot x^{1/3}} - 1\right)} \text{ as } x \to 0^+.$$

Find the exact value of the expression $\frac{tan70^{\circ}-tan20^{\circ}-2tan40^{\circ}}{tan10^{\circ}}.$ 7.

Find all values of a for which the inequality $(a - 3) x^2 - 2ax + 3a - 6 > 0$ is satisfied for all values of x. 8.





4. (i)
$$-2$$
 (ii) $e^{-\frac{a^2}{2b^2}}$

5. (i)
$$\frac{1}{2\sqrt{a}}$$
 (ii) $\frac{1}{e} \ln 2$ **6.** $a = 1, r = \frac{3}{5}, S_{\infty} = \frac{5}{2}$

7. 4 8.
$$a \in (6, \infty)$$

